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*Approximation algorithms for the normalizing constant of Gibbs distributions.*

Consider a family of distributions  $\{\pi_\beta\}$  where  $X \sim \pi_\beta$  means that  $\mathbf{P}(X = x) = \exp(-\beta H(x))/Z(\beta)$ . Here  $Z(\beta)$  is the normalizing constant for the density. Then  $\{\pi_\beta\}$  is known as a Gibbs distribution, and  $Z(\beta)$  is the partition function. This work presents new method called the paired product estimator (PPE) for approximating  $Z(\beta)$ . The PPE approximates the function to a specified level of relative accuracy using a number of samples that grows as  $O(\ln(Z(\beta)) \ln(\ln(Z(\beta))))$  when  $Z(0) \geq 1$ . This is a sharp improvement for previous, similar approaches that used a much more complicated algorithm, yet used  $O(\ln(Z(\beta)) \ln(\ln(Z(\beta)))^5)$  samples. (Received August 26, 2015)