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Almost Mathieu operator is the central quasiperiodic model in both physics and mathematics. It is given by

$$(H_{\lambda,\alpha,\theta}u)(n) = u(n+1) + u(n-1) + 2\lambda \cos 2\pi(\theta + n\alpha)u(n),$$

where λ is the coupling, α is the frequency, and θ is the phase. For fixed parameters α and λ , $\{H_{\lambda,\alpha,\theta}\}_{\theta \in \mathbb{R}}$ is a family of selfadjoint operators on $\ell^2(\mathbb{Z})$. In this talk, we study the almost Mathieu operator $\{H_{\lambda,\alpha,\theta}\}_{\theta \in \mathbb{R}}$ in localization regime, i.e., $|\lambda| > e^{\beta(\alpha)}$, where

$$\beta(\alpha) = \limsup_{n \rightarrow \infty} \frac{\ln q_{n+1}}{q_n},$$

and $\frac{p_n}{q_n}$ are the continued fraction approximants of α .

We determine the exact exponential asymptotics of eigenfunctions and of corresponding transfer matrices of the almost Mathieu operators for all frequencies and almost all phases in this regime. This also gives a constructive proof of the arithmetic version of the second transition conjecture proposed in 1994. (Received August 31, 2015)