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On the basis number of the Wreath product of graphs and some related problem.

For a given graph G , the set \mathcal{E} of all subsets of $E(G)$ forms an $|E(G)|$ -dimensional vector space over Z_2 with vector addition $X \oplus Y = (X \setminus Y) \cup (Y \setminus X)$ and scalar multiplication $1.X = X$ and $0.X = \emptyset$ for all $X, Y \in \mathcal{E}$. The cycle space, $\mathcal{C}(G)$, of a graph G is the vector subspace of $(\mathcal{E}, \oplus, .)$ spanned by the cycles of G . Traditionally there have been two notions of minimalls among bases of $\mathcal{C}(G)$. The *basis number*, $b(G)$, of G is the least non-negative integer d such that each edge of G appears in at most d edges of the basis. Second, a basis \mathcal{B} is called a *minimum cycle basis* if its total length is minimum among all bases of $\mathcal{C}(G)$.

The Wreath product $G \rho H$ has the vertex set is $V(G) \times V(H)$ and the edge set is $\{(u_1, v_1)(u_2, v_2) | u_1 = u_2 \text{ and } v_1 v_2 \in E(H), \text{ or } u_1 u_2 \in E(G) \text{ and there is } \alpha \in \text{Aut}(H) \text{ such that } \alpha(v_1) = v_2\}$. In this work, we investigate the basis number for the wreath product of some graphs. Moreover, in a related problem, we construct a minimum cycle bases of the wreath product of the same. (Received August 06, 2015)