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**Thu Dinh\*** (tndinh@cpp.edu), 3301 Yorba Linda Blvd, Apt 236, Fullerton, CA 92831. *The Repeated Sums of Integers.*

**Abstract:** It is well-known that the sum of integers from 1 to  $n$  is

$$1 + 2 + \dots + n = \frac{n(n+1)}{2}$$

But what happens when we add these sums together? Do we have a closed form formula for  $\sum_{i=1}^n \sum_{j=1}^i j = 1 + 3 + 6 +$

$\dots \frac{1}{2}n(n+1)$ ? Moreover, what happens if we keep taking the sum of the sums? In general, we will attempt to find a closed form formula for

$$\sum_{a_1=1}^n \sum_{a_2=1}^{a_1} \dots \sum_{a_m=1}^{a_{m-1}} a_m$$

We will then look at higher power of integers and repeat the process. Would we have a nice closed form formula for

$$\sum_{a_1=1}^n \sum_{a_2=1}^{a_1} \dots \sum_{a_m=1}^{a_{m-1}} a_m^k$$

for any positive power  $k$ ? The technique used in finding these sums can be used to find a formula for the partial sum of many well-known sequences. It can also be used to count the number of lattice paths under some special conditions. (Received August 16, 2015)