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Weiyong He* (whe@uoregon.edu), Department of Math, University of Oregon, Eugene, OR 97403. *Kahler-Ricci soliton and H-functional.*

We consider Kahler-Ricci solitons on a Fano manifold M . We introduce an H-functional on M ; we show that its critical point has to a Kahler-Ricci soliton and the Kahler-Ricci flow can be viewed as its reduced gradient flow. We then obtain a natural lower bound of H-functional in terms of an invariant of holomorphic vector fields on M . As an application, we prove that a Kahler-Ricci soliton, if exists, maximizes Perelman's μ -functional. Second we consider a conjecture proposed by S.K. Donaldson regarding the existence of Kahler metrics with constant scalar curvature in terms of K-energy; a simple observation is that on Fano manifolds, one can consider Donaldson's conjecture in terms of Ding's F-functional. We then state geodesic stability conjecture on Fano manifolds in terms of F-functional. Similar pictures can be naturally extended to Kahler-Ricci soliton and modified F-functional. (Received February 03, 2014)