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Jason A. Miller* (millerj@math.osu.edu), 100 Math Tower, 231 West 18th Avenue, Columbus, OH 43210. *Okounkov Bodies of Borel Orbit Closures.*

The theory of Okounkov bodies generalizes the relationship between toric geometry and polytopes. The theory associates to a valuation v and line bundle \mathcal{L} on a projective variety, a convex body $\Delta_v(\mathcal{L})$, which encodes information about the variety and line bundle. Spherical varieties are a generalization of certain classes of varieties with group actions such as toric and flag varieties. For these varieties, Okounkov theory can be used to encode information about the G -orbits via faces on an associated polytope. However, much of the structure of these varieties is determined by the Borel orbit structure which is generally not well understood. I will discuss original work examining an extension of this correspondence for a certain class of spherical varieties, wonderful group compactifications. Given any Borel orbit closure Z of a wonderful group compactification, the Okounkov construction gives a finite union of faces of the Okounkov polytope. This correspondence enjoys the same properties as in the case of G -orbits. The dimension of the space of global sections $H^0(Z, \mathcal{L})$ is given by the number of lattice points in the union of faces. One can then calculate the degree of \mathcal{L} by taking the sum of the volume of these faces. (Received June 27, 2014)