over $\mathbb{Q}$ with good reduction away from $p=3$.
Following a similar project by Smart, we describe an algorithm to determine all Picard curves over $\mathbb{Q}$ with good reduction away from 3, by establishing a correspondence between the isomorphism classes of such curves and equivalence classes of certain quintic binary forms possessing a rational linear factor. An exhaustive list of integral models is determined. As part of this algorithm, we find all $S$-unit solutions to $x+y=1$ within relevant number fields and where the finite primes in $S$ divide 3 . We include new results that apply to solving $S$-unit equations under some conditions. (Received July 29, 2014)

