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Mark Iwen* (iwenmark@msu.edu), Department of Mathematics, Michigan State University, 619 Red Cedar Road, East Lansing, MI 48824, and **Felix Krahmer**. *Fast Subspace Approximation via Greedy Least-Squares*.

I will discuss fast and deterministic dimensionality reduction techniques for a family of subspace approximation problems. Let $P \subset \mathbf{R}^N$ be a given set of M points. The techniques discussed find an $O(n \log M)$ -dimensional subspace that is guaranteed to always contain a near-best fit n -dimensional hyperplane \mathcal{H} for P with respect to the cumulative projection error $(\sum_{\mathbf{x} \in P} \|\mathbf{x} - \Pi_{\mathcal{H}} \mathbf{x}\|_2^p)^{1/p}$, for any chosen $p > 2$. The deterministic algorithm runs in $\tilde{O}(MN^2)$ -time, and can be randomized to run in only $\tilde{O}(MNn)$ -time while maintaining its error guarantees with high probability. In the case $p = \infty$ the dimensionality reduction techniques can be combined with efficient algorithms for computing the John ellipsoid of a data set in order to produce an n -dimensional subspace whose maximum ℓ_2 -distance to any point in the convex hull of P is minimized. The resulting algorithm remains $\tilde{O}(MNn)$ -time. (Received February 07, 2014)