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**Li-Chien Shen\*** ([shen@uf1.edu](mailto:shen@uf1.edu)), 358 Little Hall, Gainesville, FL 32611. *A Generalization of Ramanujan's Differential Identities for the Fundamental Automorphic Forms of the Hecke Groups.*

A Generalization of Ramanujan's Differential Identities for the Fundamental Automorphic Forms of the Hecke Groups

Abstract. Let  $m$  be a positive integer and  $\lambda = 2 \cos \frac{2\pi}{m}$ . The Hecke group  $\mathfrak{G}(\lambda)$  is the group of fractional linear transformations generated by  $\tau + \lambda$  and  $-\frac{1}{\tau}$ . Exploiting the properties of the conformal mapping for a fundamental domain of a Hecke group  $\mathfrak{G}(\lambda)$ , we construct three fundamental automorphic forms satisfying a system of differential equations. For the special case of  $\lambda = 1$ , we obtain the well-known Ramanujan's differential equations for the Eisenstein series  $P, Q$  and  $R$ :  $qP' = \frac{P^2 - Q}{12}$ ,  $qQ' = \frac{PQ - R}{3}$  and  $qR' = \frac{PR - Q^2}{2}$ . (Received February 06, 2014)