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Jon Middleton* (jmiddlet@ucsd.edu). *Hessians of Conformal Functionals as Invariant Hermitian Forms*. Preliminary report.

Let M be a compact manifold and \mathcal{M} a tame Fréchet manifold of geometric structures on M . Let $H = \text{diff}(M) \ltimes \exp(C^\infty(M))$, which acts on \mathcal{M} . A *conformal functional* F is a real-valued H -invariant function on \mathcal{M} that is twice differentiable in Hamilton's sense. The location of extrema for conformal functionals has been of interest to those in conformal geometry, in which \mathcal{M} is the space of Riemannian metrics and F is the zeta-regularized determinant of a Laplace-type differential operator.

In this talk, we will address both the space of Riemannian metrics and the space of strongly pseudoconvex CR structures on S^{2n-1} . Both spaces are acted upon by a real rank one Lie group G : $SO_0(2n, 1)$ in the former case and $SU(n, 1)$ in the latter. In each case \mathcal{M} has a distinguished structure on which these groups act conformally. We will see that these structures are critical points for F , that the Hessian of F defines a Hermitian form of an admissible representation of G , and that this representation is an irreducible $A_q(\lambda)$. (Received February 10, 2014)