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*Generalization of Bernoulli polynomials and analytic continuation of Riemann-Hurwitz zeta function.* Preliminary report.

We all know that  $f_n(k) = 1^n + 2^n + 3^n + \cdots + k^n$ ;  $n = 1, 2, \dots$  are polynomials in  $k$ . In part because  $f_n(k) = \zeta(1, -n) - \zeta(k + 1, -n)$  where  $\zeta(s, x) := \sum_{j=0}^{\infty} (s + j)^{-x}$  is Riemann-Hurwitz zeta function,  $f_n(s)$ , or  $B_n(s) := (\partial/\partial s) f_n(s - 1)$  (Bernoulli polynomials), had been under intense scrutiny. Dozen generalizations were crafted. Among all, Akiyama-Tanigawa's Pascal-like triangle (ATT) is striking. While  $B_n(s)$  reflect much of the trait of  $\zeta(s, x)$ , they alone do not have a capacity to recover  $\zeta(s, x)$ . We (1) define a double-sequence  $\{m_{i,j}(t, s)\}$  of polynomials using  $Ler(z, s, x) := \sum_{j=0}^{\infty} z^j (s + j)^{-x}$ . (2) For each  $n = 1, 2, \dots$  write  $\zeta(s, x)$  as a series involving  $m_{i,j}(t, s)$  over  $\{x; \text{Re } x > -n\}$ . This differs from the classical Euler sum and a recent work by Rubinstein. (3)  $\{(\partial^2/\partial t \partial s) m_{i,j}(t, s)|_{s=t=1}\}$  is ATT. Thus  $\zeta(1, x)$  is written as a sum involving numbers in ATT. (4) Analyze automorphisms on the algebraic curves  $C_{i,j} := \{m_{i,j}(t, s) = 0\}$  in conjunction with the functional identity for  $Ler(z, s, x)$  by Apostol and Berndt. (Received February 10, 2014)