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**Michael B Woodroffe\*** (michaelw@umich.edu). *Quenched Convergence for Normalized Sums of a Stationary Process.*

Consider a stationary Markov chain  $W_0, W_1, \dots$  with transition function  $Q$  and marginal distribution  $\pi$ ,  $Q(w, B) = P[W_{n+1} \in B | W_n = w]$  and  $\pi\{B\} = P[W_n \in B]$ . Given a  $g \in L^2(\pi)$  for which  $\int g d\pi = 0$ , let  $X_k = g(W_k)$ ,  $S_n = X_1 + \dots + X_n$ ,  $\sigma_n^2 = E(S_n^2)$ , and  $F_n(z) = P[S_n/\sigma_n \leq z]$ . Interest center on cases in which  $F_n$  converges weakly to the standard normal distribution function  $\Phi$ . In touch cases, the convergence is said to be annealed. Next, let  $G_n(w; z) = P[S_n/\sigma_n \leq z | W_0 = w]$ , so that  $D_n(w; \cdot)$  is the conditional distribution function of  $S_n/\sigma_n$  given  $W_0 = w$ . If  $G_n(w; \cdot)$  converges (weakly) to  $\Phi$  for *a.e.*  $w(\pi)$ , then the convergence is said to b quenched. Another possibility it that  $G_n(W_0; \cdot)$  converges to  $\Phi$  in probability. In this case, the convergence is said to be weakly quenched. The definitions extend directly to a stationary process  $\dots X_{-1}, X_0, X_1, \dots$  with mean 0 and finition variance by letting  $W_n = (\dots, X_{n-1} X_n)$ . Recent research on quenched convergence are known is reviewed and some new results presented. (Received July 30, 2013)