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Jozsef Balogh and **Hong Liu*** (hliu36@illinois.edu). *On the number of K_4 -saturating edges.*

Let G be a K_4 -free graph, an edge in its complement is a K_4 -saturating edge if the addition of this edge to G creates a copy of K_4 . Erdős and Tuza conjectured that for any n -vertex K_4 -free graph G with $\lfloor n^2/4 \rfloor + 1$ edges, one can find at least $(1 + o(1))\frac{n^2}{16}$ K_4 -saturating edges. We construct a graph with only $\frac{2n^2}{33}$ K_4 -saturating edges. Furthermore, we prove that it is best possible, i.e., one can always find at least $(1 + o(1))\frac{2n^2}{33}$ K_4 -saturating edges in an n -vertex K_4 -free graph with $\lfloor n^2/4 \rfloor + 1$ edges. (Received July 15, 2013)