Lucas Kramer and Ryan R. Martin* (rymartin@iastate.edu), Department of Mathematics, 396 Carver Hall, Iowa State University, Ames, IA 50010, and Michael Young. Diamond-free families in the Boolean lattice.
For a family of subsets of $\{1, \ldots, n\}$, ordered by inclusion, and a partially-ordered set $P$, we say that the family is $P$-free if it does not contain a subposet isomorphic to $P$. We want to compute $\mathrm{La}(n, P)$, the largest size of a $P$-free family of subsets of $\{1, \ldots, n\}$. It is conjectured that, for any fixed $P$, this quantity is $(k+o(1))\binom{n}{\lfloor n / 2\rfloor}$ for some fixed integer $k$, depending only on $P$. The conjecture has been verified for a number of small posets $P$ as well as posets of a "tree shape." The smallest poset for which this conjecture is open is $Q_{2}$, the Boolean lattice on two elements, also called a "diamond." We will discuss improved bounds on the size of a $Q_{2}$-free family, utilizing Razborov's flag algebra method. (Received August 06, 2013)

