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**Paul A Fuhrmann\*** (fuhrmannbgu@gmail.com) and **Uwe Helmke**. *Open loop control for state systems*. Preliminary report.

Given a discrete-time, reachable linear system, in state space form  $(zI - A)x(z) = Bu(z)$ , initially at rest. Our aim is to compute controls that steer the system to a prescribed state  $\xi$ . The reachability map is defined by  $\mathcal{R}_{(A,B)}u = \pi_{zI-A}Bu$  for  $u(z) \in \mathbb{F}[z]^m$ , which is a surjective  $\mathbb{F}[z]$  homomorphism. We note that  $\mathcal{R}_{(A,B)}$  has a kernel which is a full submodule, hence representable as  $D\mathbb{F}[z]^m$  for a nonsingular  $D(z)$ . Factoring out the kernel, we get the reduced reachability map given by  $\mathcal{R} = \mathcal{R}_{(A,B)}|X_D$ . By construction  $\mathcal{R}$  is an isomorphism and we invert it by embedding the intertwining relation  $BD(z) = (zI - A)H(z)$  the following doubly coprime factorization

$$\begin{pmatrix} Y(z) & X(z) \\ -B & zI - A \end{pmatrix} \begin{pmatrix} D(z) & -X'(z) \\ H(z) & Y'(z) \end{pmatrix} = \begin{pmatrix} I & 0 \\ 0 & I \end{pmatrix}.$$

In this case we have  $u_m(z) = \mathcal{R}^{-1}\xi = \pi_D X'\xi$ .

Extensions to some standard networks of linear systems will be indicated.

**Key words:** Linear systems, controllability, open loop control, unimodular embedding.

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