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Tamás Kálmán* (kalman@math.titech.ac.jp). *Tutte's polynomial for hypergraphs and polymatroids.*

Given an integer-valued submodular set function μ , I will define two polynomial invariants of the corresponding polymatroid that generalize the valuations $T(x, 1)$ and $T(1, y)$ of the Tutte polynomial of matroids. The definitions use extensions of Tutte's notions of internal and external activity to the integer lattice points in the base polytope B_μ . I will state several properties of the new polynomials (including deletion-contraction formulas and a conjectural relation to the h -vector of root polytope triangulations) for a class of polymatroids derived from hypergraphs. If we further specialize to hypergraphs that can be drawn as plane bipartite graphs, we obtain a version of the planar duality rule for T , as well as a connection to Tutte's Tree Trinity Theorem. Some of these results are joint with Alex Postnikov. (Received July 27, 2011)