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**Eunkyung Ko\*** (ek94@msstate.edu), 319 N.Jackson st. 1A, Starkville, MS 39759. *Uniqueness and multiplicity results for classes of infinite positive problems.*

We study positive solutions to the singular boundary value problem

$$\begin{aligned} -\Delta u &= \lambda \frac{f(u)}{u^\beta} && \text{in } \Omega, \\ u &= 0 && \text{on } \partial\Omega, \end{aligned}$$

where  $\lambda$  is a positive parameter,  $\beta \in (0, 1)$  and  $\Omega$  is a bounded domain in  $\mathbb{R}^N$ ,  $N \geq 1$ . Here  $f \in C([0, \infty), (0, \infty))$  is nondecreasing and satisfies  $\lim_{u \rightarrow \infty} \frac{f(u)}{u^{\beta+1}} = 0$ . We discuss the existence of multiple positive solutions for a certain range of  $\lambda$  and a uniqueness result for  $\lambda \gg 1$ . A simple model that will satisfy our hypotheses is  $f(u) = e^{\frac{\alpha u}{\alpha+u}}$  for  $\alpha \gg 1$ . We extend our multiplicity result to classes of systems, including  $p$ -Laplacian systems, when the nonlinearities satisfy certain combined sublinear conditions at infinity. We also extend our results to the case when  $\Omega$  is an exterior domain. (Received July 21, 2011)