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Daniel W. Cranston* (dcranston@vcu.edu) and **Gexin Yu.** *Linear Choosability of Sparse Graphs.*

A linear coloring is a proper coloring such that each pair of color classes induces a union of disjoint paths. We study the linear list chromatic number, denoted $lc_\ell(G)$, of sparse graphs. The maximum average degree of a graph G , denoted $mad(G)$, is the maximum of the average degrees of all subgraphs of G . It is clear that any graph G with maximum degree $\Delta(G)$ satisfies $lc_\ell(G) \geq \lceil \Delta(G)/2 \rceil + 1$. In this paper, we prove the following results: (1) if $mad(G) < 12/5$ and $\Delta(G) \geq 3$, then $lc_\ell(G) = \lceil \Delta(G)/2 \rceil + 1$, and we give an infinite family of examples to show that this result is best possible; (2) if $mad(G) < 3$ and $\Delta(G) \geq 9$, then $lc_\ell(G) \leq \lceil \Delta(G)/2 \rceil + 2$, and we give an infinite family of examples to show that the bound on $mad(G)$ cannot be increased in general; (3) if G is planar and has girth at least 5, then $lc_\ell(G) \leq \lceil \Delta(G)/2 \rceil + 4$. (Received July 24, 2011)