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Let  $A$  be a compact infinite metric space with metric  $m$  and let  $\omega_N = \{x_i\}_{i=1}^N \subset A$  denote a configuration of  $N \geq 2$  points in  $A$ . The *separation distance* of  $\omega_N$  is

$$\delta(\omega_N) := \min_{1 \leq i \neq j \leq N} (x_i, x_j),$$

and the *mesh norm* (covering radius) of  $\omega_N$  with respect to  $A$  is

$$\rho(\omega_N, A) := \max_{y \in A} \min_{1 \leq i \leq N} (y, x_i).$$

An  $N$ -point *best-packing configuration*  $\omega_N^*$  is a configuration such that

$$\delta_N(\omega_N^*) := \max\{\delta(\omega_N) : \omega_N \subset A, |\omega_N| = N\}.$$

We investigate upper and lower bounds for the *mesh-separation ratio* (or *mesh-ratio*)

$$\gamma(\omega_N^*, A) := \rho(\omega_N^*, A) / \delta(\omega_N^*).$$

Furthermore, we study this quantity for best-packing configurations that are the limits of  $N$ -point minimal Riesz  $s$ -energy configurations. For the sphere  $S^2 \subset \mathbb{R}^3$  we show that for  $N = 5$  the limit of such  $s$ -energy configurations as  $s \rightarrow \infty$  is the pyramid with square base (the 5-point best-packing configuration that has the maximum number of equal-distance pairs). (Received December 09, 2011)