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Duality in Segal-Bargmann Spaces.

The Segal-Bargmann space is the holomorphic L^2 space of Gaussian measure γ on \mathbb{C}^n . As a Hilbert space, it is (of course) self-dual. The corresponding holomorphic L^p spaces for $p \neq 2$ have more complicated duality relations. It has been known since the mid-80s that the dual to $L^p_{hol}(\gamma)$ can be identified with $L^{p'}(\gamma_p)$ for the conjugate exponent $\frac{1}{p} + \frac{1}{p'} = 1$ and a *dilated* Gaussian measure γ_p ; but this is not isometric.

Here we will present a tight estimate on constant of comparison between the dual norms. It grows exponentially fast with dimension n , leaving open many interesting questions about L^p Segal-Bargmann spaces in infinite-dimensions. The key to the proof is viewing $L^p_{hol}(\gamma)$ as a space of holomorphic sections over a(n in this case trivial) vector bundle; this point of view shows why the dilation of the measure is natural, and translates the problem to the L^p -norm of an orthogonal projection. (Received December 13, 2011)