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Madison, WI 53706. *High-performance very local Riesz wavelet bases of $L_2(\mathbb{R}^d)$.*

We introduce new methodologies for the construction of high-performance very local Riesz wavelet bases of $L_2(\mathbb{R}^d)$ in arbitrarily high spatial dimension d . The localness L of the representation is measured as the sum of the volumes of the supports of the underlying mother wavelets; small localness number is one of the sought-for properties in wavelet constructions. Our constructs are very simple and they are based on the framelet construction methods known as the CAMP scheme and the L-CAMP scheme. Within our general methodology, the subclass of piecewise-constant constructions is the most local one. It includes Riesz wavelet bases with any performance grade and in any spatial dimension. In this subclass, the Riesz wavelet basis with Jackson-type performance k (namely, with k vanishing moments) has localness score $L < k + 1$, independently of the spatial dimension d . Thus, while the number of mother wavelets grows exponentially fast with the dimension, the sum of their volumes remains bounded. In comparison, the widely used d -dimensional tensor-product Daubechies' system with k vanishing moments has localness score $L \approx (4k - 2)^d$. (Received December 11, 2011)