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**M I Elashiry** and **D S Passman\*** ([passman@math.wisc.edu](mailto:passman@math.wisc.edu)), Department of Mathematics, 603 Van Vleck Hall, University of Wisconsin, Madison, WI 53706. *Rewritable groups.*

A group  $G$  is said to satisfy the  $n$ -permutational property  $P_n$  if for all  $n$ -tuples  $(g_1, g_2, \dots, g_n)$  of group elements, there exists a nonidentity permutation  $\sigma \in \text{Sym}_n$  (depending upon the  $n$ -tuple) with  $g_1 g_2 \cdots g_n = g_{\sigma(1)} g_{\sigma(2)} \cdots g_{\sigma(n)}$ . Similarly,  $G$  satisfies the  $n$ -rewritable property  $Q_n$  if for all  $n$ -tuples  $(g_1, g_2, \dots, g_n)$ , there exist distinct permutations  $\sigma, \tau \in \text{Sym}_n$  with  $g_{\sigma(1)} g_{\sigma(2)} \cdots g_{\sigma(n)} = g_{\tau(1)} g_{\tau(2)} \cdots g_{\tau(n)}$ . Obviously,  $P_n$  implies  $Q_n$ , but it is known that the converse is not true. Here we prove a conjecture of Blyth that  $Q_n$  implies  $P_m$ , where  $m$  is a fixed function of  $n$ . For this, we first show that there exist finite-valued functions  $a(n)$  and  $b(n)$  so that if  $G$  satisfies  $Q_n$ , then  $G$  has a characteristic subgroup  $N$  such that  $|G : N| \leq a(n)$  and  $|N'| \leq b(n)$ . The conjecture then follows with  $m = a(n)(b(n) + 1)$ . (Received November 29, 2011)