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**Katherine E Stange\*** ([stange@math.stanford.edu](mailto:stange@math.stanford.edu)), Stanford University Mathematics, 450 Serra Mall, Bldg 380, Stanford, CA 94305. *Integral points on elliptic curves and explicit valuations of division polynomials.*

Assuming Lang's conjectured lower bound on the heights of non-torsion points on an elliptic curve, we show that there exists an absolute constant  $C$  such that for any elliptic curve  $E/\mathbb{Q}$  and non-torsion point  $P \in E(\mathbb{Q})$ , there is at most one integral multiple  $[n]P$  such that  $n > C$ . The proof is a modification of a proof of Ingram giving an unconditional but not uniform bound. The new ingredient is a collection of explicit formulæ for the sequence  $v(\Psi_n)$  of valuations of the division polynomials. For  $P$  of non-singular reduction, such sequences are already well described in most cases, but for  $P$  of singular reduction, we are led to define a new class of sequences called *elliptic troublemaker sequences*, which measure the failure of the Néron local height to be quadratic. As a corollary in the spirit of a conjecture of Lang and Hall, we obtain a uniform upper bound on  $\widehat{h}(P)/h(E)$  for integer points having two large integral multiples. (Received December 13, 2011)