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278-8510. *On inverse Galois problem with certain prime conditions*. Preliminary report.

We solve the inverse Galois problem with certain prime splitting conditions. For a positive integer  $n$  let  $K$  be a number field with degree  $n$  such that every prime divisor of  $n$  remains prime in  $K$ . It is known that such a field  $K$  is non-Galois if  $n$  is divisible by 8. We study the Galois group of the Galois closure of such  $K$ . Let  $G$  be a subgroup of the  $n$ th symmetric group  $S_n$  containing a permutation of length  $n$ . When  $n$  is not greater than 8 and  $G$  is not the 8th cyclic group  $C_8$ , we prove that there exists a number field  $K$  with degree  $n$  such that every prime divisor of  $n$  remains prime in  $K$  and the Galois group of the Galois closure of  $K$  is isomorphic to  $G$ . We verify the existence of  $K$  by an explicit polynomial defining  $K$ . (Received December 11, 2011)