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**Joel Berman\*** (jberman@uic.edu). *Characterizations of maximal-sized  $n$ -generated algebras*. Preliminary report.

For  $n$  a positive integer and  $K$  a finite set of finite algebras, let  $\mathbf{L}(n, K)$  denote the largest  $n$ -generated subdirect product whose subdirect factors are algebras in  $K$ . For every  $n$  and  $K$  we provide an upper bound on the cardinality of  $\mathbf{L}(n, K)$ . This upper bound depends only on  $n$  and basic numerical parameters involving the subalgebras, automorphisms and congruence relations of the algebras in  $K$ . Let  $\mathcal{V}$  denote the variety generated by  $K$ . We provide several characterizations of when the free algebra for  $\mathcal{V}$  on  $n$  free generators has cardinality equal to  $|\mathbf{L}(n, K)|$ . One characterization is in terms of basic algebraic properties of  $\mathcal{V}$  and of the algebras in  $K$ . The second involves the term operations for members of  $K$ . The third characterization, and the one that will be emphasized in this talk, is based on specific computational tests involving the algebras in  $K$ . (Received November 18, 2011)