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**David E. Dobbs, Ronald Levy and Jay Shapiro\***, jshapiro@gmu.edu. *A universal survival ring of continuous functions which is not a universal lying-over ring.*

Part II is devoted to constructing an infinite-dimensional US-ring  $R$  which is not a ULO-ring. In fact,  $R$  can be taken to be the ring of continuous real-valued functions on the one-point compactification of the discrete space of cardinality  $\aleph_1$ . This ring  $R$  is also shown to have the following properties. Not only is  $R$  infinite-dimensional, but there exist chains of cardinality  $\mathfrak{c}$  that consist of prime ideals of  $R$ . Moreover,  $R/P$  is a divided domain for each  $P \in \text{Spec}(R)$ . If the Continuum Hypothesis holds, then there exists a minimal prime ideal  $P$  of  $R$  such that  $R/P$  is an infinite-dimensional valuation domain; however, it is consistent with ZFC that no such minimal primes exist. (Received January 17, 2011)