1062-17-165 Eric Sommers* (esommers@math.umass.edu), Department of Mathematics and Statistics, University of Massachusetts, LGRT, Amherst, MA 01003. Exterior powers of the reflection representation in Springer theory.

We will discuss the structure of the W-invariants in $H^*(\mathcal{B}_e) \otimes \wedge^* V$, where \mathcal{B}_e is the Springer fiber over the nilpotent element e in a simple Lie algebra \mathfrak{g} . Here, W is the Weyl group acting on the cohomology of the fiber via Springer theory and V is the reflection representation of W. This is closely related to a conjecture of Lehrer and Shoji when e is regular in a Levi subalgebra. This conjecture was proved by Henderson in types A, B, C.

We establish the Lehrer-Shoji conjecture in the remaining types (and discuss and prove an extension of the conjecture to all e). We will also discuss a connection to rational Cherednik algebras, which leads to a graded decomposition of the representation of W on L/tL, where L is the coroot lattice and t is a natural number prime to the Coxeter number h. (Received August 05, 2010)