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Jeffrey M Riedl* (riedl@uakron.edu), Department of Mathematics, 302 Buchtel Common, University of Akron, Akron, OH 44325-4002. *Duality for normal subgroups of wreath product p -groups*. Preliminary report.

Let B denote the direct product of n copies of the cyclic group of order m . For each subgroup N of B there is a natural way (related to the character theory of B) to define a particular subgroup of B that we denote as N^\perp . This map $N \mapsto N^\perp$ is inclusion-reversing and satisfies $|N| \cdot |N^\perp| = |B|$ and $(N^\perp)^\perp = N$. Because of this last condition, we call N^\perp the "dual" of N in B . For each group H that acts via automorphisms on B , the dual of every H -invariant subgroup of B is easily seen to be H -invariant.

Now fix a prime p and an integer $d \geq 2$. Taking $n = p^d$ and $m = p^2$, we may regard B as the base group for the regular wreath product group W of the cyclic group of order p^2 by the cyclic group of order p^d . Let \mathcal{N} denote the set of all normal subgroups of W that are contained in B , and note that for each $N \in \mathcal{N}$ we have $N^\perp \in \mathcal{N}$. We have previously obtained a detailed description of all the members of the set \mathcal{N} . In this talk we present a result that describes in some detail how the dual map $N \mapsto N^\perp$ behaves on the set \mathcal{N} . (Received September 13, 2010)