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**Kent G Slinker\*** ([kslinker@pima.edu](mailto:kslinker@pima.edu)), 1033A North 3rd Ave, Tucson, AZ 85705. *An Infinitude of Primes of the Form  $b$  squared plus one.*

If  $b^2 + 1$  is prime then  $b$  must be even, hence we examine the form  $4u^2 + 1$ . Rather than study primes of this form we study composites where the main theorem of this paper establishes that if  $4u^2 + 1$  is composite, then  $u$  belongs to a set whose elements are those  $u$  such that  $u^2 + t^2 = n(n + 1)$ , where  $t$  has a upper bound determined by the value of  $u$ . This connects the composites of the form  $4u^2 + 1$  with numbers expressible as the sum of two squares equal to the product of two consecutive integers. A result obtained by Gauss concerning the average number of representations of a number as the sum of two squares is then used to show that an infinite sequence of  $u$  for which  $u^2 + t^2 = n(n + 1)$  is impossible. This entails the impossibility of an infinite sequence of composites, and hence an infinitude of primes of the form  $b^2 + 1$ .

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