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In earlier work we proved that every distribution or hyperfunction in R^m can be obtained as a boundary value $f(x+0) - f(x-0)$ of a function $f(x+xo)$ in $R^{m+1} \setminus R^m$ which satisfies the generalized Cauchy-Rieman equation $(\partial xo + \partial x)f(x+xo) = 0$ for monogenic functions.

In particular the delta distribution $d(x)$ is the boundary value of the Cauchy kernel $E(x+xo) = 1/(Am+1)(xo-x)/|x+xo|^{m+1}$.

Microlocalisation involves a kind of non-linear Radon transform by which the delta distribution is decomposed further into distributions $D(x, w)$ which are singular in the origin and in the direction w (w belongs to the unit sphere); these functions are used to study wavefront sets and micro-supports. In our presentation we illustrate that this classical microlocal decomposition of the delta-distribution can be obtained by using boundary values of monogenic functions as opposed to functions of several complex variables. As a side result we obtain the formula $d(x) = 2/(Am+1)[(1-ax)(xo-x)/|xo+x|^{m+1}]_o$ whereby the notation $[.]_o$ refers to the scalar part and $xo+x$ belongs to the parabola $xo = a|x|^2$. (Received September 11, 2009)