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Mark D Haiman^{*}, Department of Mathematics, 970 Evans Hall, University of California, Berkeley, CA 94720-3840, and Li-Chung Chen. *k-Schur functions, graded* S_n modules, and the flag variety. Preliminary report.

I'll give an overview of some conjectures of mine, and some theorems and conjectures of my student Li-Chung Chen, which lead to several (conjecturally equivalent) descriptions for a family of q-symmetric functions which we conjecture to include the k-Schur functions of Lascoux, Lapointe and Morse. One description is representation-theoretic, a second is combinatorial, and the third is an explicit formula which comes from a geometric interpretation. The package of conjectures offers a possible explanation for the various positivity properties that k-Schur functions are expected to satisfy. (Received February 06, 2009)