

1048-05-127

Matthias Beck* (beck@math.sfsu.edu), Department of Mathematics, San Francisco State University, San Francisco, CA 94132, and **Alan Stapledon**, Department of Mathematics, University of Michigan, Ann Arbor, MI 48109. *Asymptotics of Ehrhart series of Lattice Polytopes.*

If P is a lattice polytope (i.e., P is the convex hull of finitely many integer points in \mathbf{R}^d), Ehrhart's theorem asserts that the integer-point counting function $L_P(m) = \#(mP \cap \mathbf{Z}^d)$ is a polynomial in the integer variable m . Equivalently, the generating function $Ehr_P(t) = \sum_{m \geq 0} L_P(m)t^m$ is a rational function of the form $h(t)/(1-t)^{d+1}$; we call $h(t)$ the Ehrhart h-vector of P . We study the behavior of the Ehrhart series $Ehr_{nP}(t) = \sum_{m \geq 0} L_P(nm)t^m$ as n grows; e.g., we can prove that the Ehrhart h-vector of nP is eventually unimodal, where "eventually" only depends on the dimension of P . Our results are general combinatorial theorems about generating functions and can be applied to other settings, e.g., Veronese subrings of graded rings. (Received February 03, 2009)