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**Maya Chhetri\*** (maya@uncg.edu), Department of Mathematics and Statistics, 125 Petty Science Bldg, UNC Greensboro, Greensboro, NC 27402, and **Petr Girg**. *Existence and Nonexistence of Positive Solutions For a Class of Superlinear Semipositone Systems.*

We consider an elliptic system of the form

$$\left. \begin{aligned} -\Delta u &= \lambda f(v) & \text{in } \Omega \\ -\Delta v &= \lambda g(u) & \text{in } \Omega \\ u = 0 = v & & \text{on } \partial\Omega, \end{aligned} \right\}$$

where  $\lambda > 0$  is a parameter,  $\Omega$  is a bounded domain in  $R^N$  with smooth boundary  $\partial\Omega$ . The nonlinearities  $f, g : [0, \infty) \rightarrow R$  are  $C^1$  functions that are superlinear at infinity and satisfy  $f(0) < 0$  and  $g(0) < 0$ . We prove that the system has a positive solution for  $\lambda$  small when  $\Omega$  is convex with  $C^3$  boundary and no positive solution for  $\lambda$  large when  $\Omega$  is a general bounded domain with  $C^{2,\beta}$  boundary.

We use fixed point index combined with re-scaling argument to prove the existence result while positive solutions are analyzed in a sub-domain near the boundary to prove the nonexistence result. (Received September 01, 2008)