

1026-60-100

Elena Kosygina* (elena_kosygina@baruch.cuny.edu), One Bernard Baruch Way, Box B6-230, New York, NY 10010, and **Srinivasa R. S. Varadhan.** *Homogenization of Hamilton-Jacobi-Bellman equations with respect to time-space shifts in a stationary ergodic random medium.*

We consider a family $\{u_\epsilon(t, x, \omega)\}$, $\epsilon > 0$, of solutions of the final value problem

$$\frac{\partial u_\epsilon}{\partial t} + \frac{\epsilon}{2} \Delta u_\epsilon + H\left(\frac{t}{\epsilon}, \frac{x}{\epsilon}, \nabla u_\epsilon, \omega\right) = 0, \quad u_\epsilon(T, x, \omega) = U(x),$$

where the time-space dependence of the Hamiltonian $H(t, x, p, \omega)$ is realized through the shifts in a stationary ergodic random medium. For Hamiltonians, which are convex in p and satisfy certain growth and regularity conditions, we show the almost sure locally uniform in time and space convergence of $u_\epsilon(t, x, \omega)$ as $\epsilon \rightarrow 0$ to the solution $u(t, x)$ of a deterministic “effective” equation

$$\frac{\partial u}{\partial t} + \bar{H}(\nabla u) = 0, \quad u(T, x) = U(x).$$

The averaged Hamiltonian $\bar{H}(p)$ is given by a variational formula. (Received February 19, 2007)