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**Tamon Stephen\*** ([tamon@sfu.ca](mailto:tamon@sfu.ca)), Department of Mathematics, Simon Fraser University, Surrey, B.C. V3M 0A3, Canada. *Colourful Simplicial Depth*.

The simplicial depth of a point  $p$  in  $\mathbb{R}^d$  with respect to a finite set  $S$  of points is the number of  $d + 1$ -sets from  $S$  whose convex hull contains  $p$ . In statistics, this is a measure of how well  $p$  represents  $S$ .

A natural generalization is to colour the points of  $S$  and consider only the colourful simplices containing  $p$ . We exhibit a configuration where  $p$  is in the convex hull of each of  $d + 1$  colours, but is only in  $d^2 + 1$  colourful simplices. We conjecture that this is minimal and prove a quadratic lower bound. This result sharpens Bárány's Colourful Carathéodory Theorem, and gives an improved lower bound for monochrome simplicial depth. (Received August 09, 2008)