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Let  $\lambda(k)$  denote the Liouville lambda function, the completely multiplicative function defined by  $\lambda(p) = -1$  for every prime  $p$ . In 1919, Pólya noted that the Riemann hypothesis follows if the sum  $L(n) = \sum_{k=1}^n \lambda(k)$  does not change sign for large  $n$ , and in 1948 Turán noted a similar property for the function  $T(n) = \sum_{k=1}^n \lambda(k)/k$ . In 1958, Haselgrove proved that both  $L(n)$  and  $T(n)$  change sign infinitely often, without determining any precise values where a sign change occurs. In 1960, Lehman found an integer  $n_0 > 1$  where  $L(n_0) > 0$ , but no specific integer  $n_1$  had been found where  $T(n_1) < 0$ . We describe a recent large computation that has determined the smallest such integer. (Received January 03, 2007)