

1018-11-134

Hung-ping Tsao*, 1151 Highland Drive, Novato, CA 94949. *Relationships of powered sums of an arithmetic progression among different powers.*

Let $S(n;k)$ be the k -powered sum of $a, a+d, a+2d, \dots, a+(n-1)d$. Then the polynomial expression in n of $S(n;k)$ can be obtained via $S(n;k) = d[n + (a/d)]S(n;k-1) - [S(1;k-1) + S(2;k-1) + \dots + S(n;k-1)]$, which can also be used to prove the closed form for $S(n;k)$ already established [Abstract #1012-11-11] by the mathematical induction on k . The least-square-fit polynomial regression formulas for any equally spaced observed data can be substantially simplified by virtue of relationships among $S(n;k)$'s. For example, the quadratic formula of this kind can be obtained due to the fact that $S(n;4)S(n;2) - S(n;3)S(n;3)$, $S(n;4)S(n;1) - S(n;3)S(n;2)$, $S(n;4)S(n;0) - S(n;2)S(n;2)$, $S(n;3)S(n;1) - S(n;2)S(n;2)$ and $S(n;3)S(n;0) - S(n;2)S(n;1)$ all have the common factor $d(dn/2)C(n+1,3)$, with $C(n+1,3)$ being a binomial coefficient. (Received March 06, 2006)