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Christopher A. Francisco* (chrisf@math.missouri.edu), Department of Mathematics, Univ. of Missouri, 202 Mathematical Sciences Building, Columbia, MO 65211, and **Adam Van Tuyl**.

Some families of componentwise linear ideals. Preliminary report.

Let $J = \{j_1, \dots, j_t\}$ be a subset of $[n] = \{1, \dots, n\}$, and let \mathfrak{m}_J be the ideal $(x_{j_1}, \dots, x_{j_t})$ in $R = k[x_1, \dots, x_n]$. We will discuss ideals of the form $I = \mathfrak{m}_{J_1}^{a_1} \cap \dots \cap \mathfrak{m}_{J_s}^{a_s}$, where the J_i are subsets of $[n]$. These ideals arise naturally in a number of settings, including as ideals of some sets of fat points, as ideals of tetrahedral curves, and in combinatorics when all $a_i = 1$. We will identify a number of cases in which these ideals are componentwise linear by using the theory of polymatroidal ideals, and we will discuss some applications. (Received August 04, 2005)