Jacques Verstraete\* (jverstra@math.uwaterloo.ca), Faculty of Mathematics, University of Waterloo, Waterloo, N2L 3G1, Canada. Product Representations of Polynomials.

In this talk I will discuss the algorithmic problem of efficiently determining the existence of a linear dependence amongst a set of vectors in a finite dimensional vector space over  $F_q$ . To do so, a more general framework is introduced, where we look for integer factorizations of points in the value set of a polynomials.

For a polynomial  $f \in Z[X]$  and positive integers k and N, let  $\rho_k(N; f)$  denote the maximum size of a set  $A \subset \{1, 2, ..., N\}$  such that no product of k distinct elements of A is in the value set of f.

Using a little algebraic geometry, the probabilistic method and some extremal combinatorics, we prove that for every polynomial f of prime degree d, either  $\rho_k(N; f)$  is linear in N, or |f| is the  $d^{\text{th}}$  power of a monic linear polynomial and  $\rho_k(N; f) \sim c\pi(N) + O(N^{1-1/2d})$  and c is completely determined. This generalizes earlier results of Erdős (1963), Erdős, Sós and A. Sárközy (1995), Györi and G. Sárközy (1997). We conclude with some open questions. (Received August 07, 2005)