

**Meeting:** 999, Nashville, Tennessee, SS 7A, Special Session on Operator Theory on Function Spaces

999-47-35                    **Morteza Seddighin\*** (mseddigh@indiana.edu), Mathematics Department, Indiana University  
East, Richmond, IN 47374. *A Generalization of Kantorovich Inequality to two Operators.*

Given a positive operator  $T$ , let  $m$  and  $M$  be the smallest and largest eigenvalues of  $T$  respectively. It is proved by Kantorovich that the first antieigenvalue of  $T$  or  $\cos T$  is equal to the ratio of the geometric mean of  $m$  and  $M$  to arithmetic mean of these two numbers. We will generalize the Kantorovich Inequality to interactive antieigenvalue  $\cos(S, T)$  between two positive operators  $T$  and  $S$ . More precisely, will establish various upper and lower bounds for  $\cos(S, T)$  in terms of smallest and largest eigenvalues of  $S$  and  $T$ . Will show that in fact one of these inequalities is sharper than Strang bound for  $\cos(S, T)$ . (Received July 16, 2004)